

# Standard Form of Quadratic: $y = ax^2 + bx + c$

Unit 7: Quadratics- Families of Parabolas

Classwork

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Key

Use a graphing calculator to explore the relationship for each of the following groups of parabolas.

I. Exploring effects of changing the coefficient (a) in  $y = ax^2 + c$

1. Which of the following parabolas is the narrowest (most vertically stretched).

A.  $y = x^2$

B.  $y = 2x^2$

C.  $y = 3x^2$

D.  $y = 4x^2$

2. Which of the following parabolas is the narrowest (most vertically stretched).

A.  $y = x^2$

B.  $y = \frac{1}{2}x^2$

C.  $y = \frac{1}{3}x^2$

D.  $y = \frac{1}{4}x^2$

Now, explain what you discovered about the effects of changing the coefficient of  $x^2$ ?

The greater the coefficient of  $x^2$ , 'a', the narrower the parabola.  
The smaller the 'a' the wider the parabola.

3. Which of the following parabolas opens up?

A, B positive 'a'

4. Which of the following parabolas opens down?

C, D negative 'a'

A.  $y = x^2$

B.  $y = 3x^2$

C.  $y = -2x^2$

D.  $y = -\frac{1}{4}x^2$

Now explain what you discovered about the effect of changing the sign of the coefficient of  $x^2$ ?

If coefficient of  $x^2$  is positive the parabola opens up.  
If coefficient of  $x^2$  is negative the parabola opens down.

II. Exploring the effect of changing the constant (c) in  $y = ax^2 + c$

5. Give the **minimum** value **for y** (y-value of the vertex) for each function. *only when bx is zero*

A.  $y = x^2 + 0$

B.  $y = x^2 + 1$

C.  $y = 2x^2 + 3$

D.  $y = \frac{1}{4}x^2 - 4$

min 0

min 1

min 3

min -4

6. Give the **maximum** value **for y** (y-value of the vertex) for each function.

A.  $y = -x^2$

B.  $y = -x^2 + 1$

C.  $y = -2x^2 + 3$

D.  $y = -\frac{1}{4}x^2 - 4$

max 0

max 1

max 3

max -4

Now explain what you discovered about the vertex (minimum or maximum) of the graph of a quadratic function? *The minimum or maximum*

*was the value of 'c'*

7. How can you tell if it is a minimum or maximum?

*It's a minimum if the coefficient of  $x^2$  is positive*  
*It's a maximum if the coefficient of  $x^2$  is negative*

8. **Without** a calculator, determine the vertex for each graph and state if it gives a maximum or minimum value for y. Then use a graphing calculator to check your answers.

A.  $y = 4x^2$

B.  $y = -x^2 + 3$

C.  $y = x^2 - 5$

D.  $y = -6x^2 + 8$

Vertex: (0,0)  
min/max: min

Vertex: (0,3)  
min/max: max

Vertex: (0,-5)  
min/max: min

Vertex: (0,8)  
min/max: max

Summary: fill in the blanks describing the effects that a and c have on the graph  $y = ax^2 + c$

If a is greater than 1 the graph gets narrower

If a is less than 1 the graph gets wider

If c is positive then the graph shifts up

If c is negative then the graph shifts down