

## II. Multiplying with Radicals

When multiplying radicals, you must multiply the numbers outside the radicals AND then multiply the numbers inside the radicals.

~~-Then Simplify!!!~~

Example:

$$O_1\sqrt{I_1} \cdot O_2\sqrt{I_2} = O_1 \cdot O_2 \cdot \sqrt{I_1 \cdot I_2} \quad \left. \begin{array}{l} \text{ } \\ \text{ } \end{array} \right\} \sqrt{6} (\sqrt{6} - \sqrt{2})$$

$$2\sqrt{3} * 4\sqrt{5} = 2 * 4 * \sqrt{(3 * 5)} = 8\sqrt{15}$$

$$\sqrt{36} - \sqrt{12}$$

$$\boxed{\sqrt{6} - 2\sqrt{3}}$$

Use the FOIL method when multiplying two expressions with radicals that cannot be simplified into a monomial.

$$(6 - \sqrt{5})(3 + \sqrt{5}) = F \quad O \quad I \quad L$$

6	$-\sqrt{5}$		
3	18	$-3\sqrt{5}$	
$+\sqrt{5}$	6 $\sqrt{5}$	-5	
$- \sqrt{5} \cdot 5$			

$$\begin{aligned}
 &= (6)(3) + (6)(\sqrt{5}) + (-\sqrt{5})(3) + (-\sqrt{5})(\sqrt{5}) \\
 &= 18 + 6\sqrt{5} \quad - 3\sqrt{5} \quad - 5 \\
 &= \boxed{13 + 3\sqrt{5}}
 \end{aligned}$$

### NOW YOU PRACTICE:

Simplify the following expressions:

1)  $(4 + \sqrt{3})(4 - \sqrt{3})$

F O I L       $16 - 4\sqrt{3} + 4\sqrt{3} - \sqrt{9} = \boxed{13}$

$$\sqrt{24} = \sqrt{2^2 \cdot 6} = 2\sqrt{6}$$

2)  $(6 - \sqrt{10})(3 + \sqrt{20})$

$$2\sqrt{5}$$

6	$-\sqrt{10}$		
3	18	$-3\sqrt{10}$	
$2\sqrt{5}$	12 $\sqrt{5}$	$-2\sqrt{50}$	$-10\sqrt{2}$

5.  $-2\sqrt{50}$

$2\sqrt{25} = 2 \cdot 5 = 10$

$$(18 - 10\sqrt{2} + 12\sqrt{5} - 3\sqrt{10})$$

4)  $(2 - \sqrt{6})(2 - \sqrt{6})$

$$= \boxed{10 - 4\sqrt{6}}$$

5)  $(\sqrt{2} - \sqrt{3})(\sqrt{3} + \sqrt{5})$

F O I L       $\sqrt{6} + \sqrt{10} - 3 - \sqrt{15}$

$$\boxed{-3 + \sqrt{6} + \sqrt{10} - \sqrt{15}}$$

2	$-\sqrt{6}$		
-1	4	$-2\sqrt{6}$	
	$-2\sqrt{6}$	$\sqrt{15}$	6